Introduction to Scientific Computing Languages

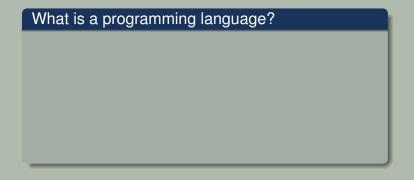
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- A set of instructions and constructs to communicate with a computing device
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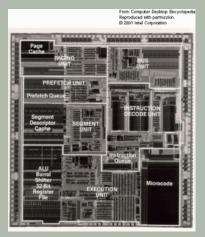
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What is a programming language?

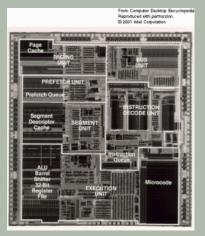
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What is a "computing device"?

sequential processors, embedded processors, ..., parallel computers, supercomputers.



Arithmetic Logic Unit (ALU) (control signals, inputs, outputs), Floating Point Unit (FPU), Prefetching Unit, Registers, . . .



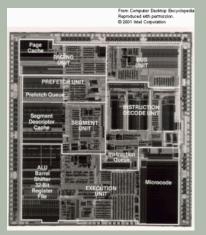
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- Languages let the users specify how to use these components
- Only **Assembly** operates on components: "low-level" language
- "High-level" languages only specify the computations to be performed
- A compiler and/or an interpreter translates high-level programs into a sequence of component actions

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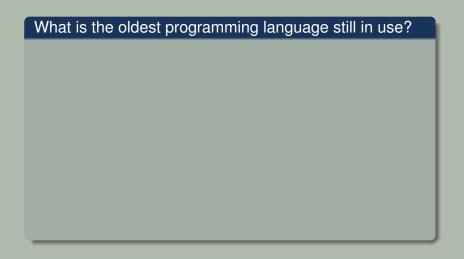
- Very fast!
- Not the lowest level. Not directly executable.
- Assembler translates assembly into machine code. Executable.
- Assembly consists of mnemonic codes.
 Machine code: only numbers.
- Translation Assembly
 ← machine code is almost 1-1.
 This is not true for high-level languages.
- Assembler is hardware-specific. Control over chips' components.

Example

```
.text
      .globl poly
poly:
      li.s $f0, 0.0
                          # y = 0, running & return result
      mtc1 $6 $f12
                          # x, move to float register
Loop:
      mul.s $f14, $f12, $f0 # compute (x * y)
      mul $2, $5, 4 # $5 = i, compute address of a[i]
      addu $3, $2, $4 # a + (i*4)
      1.s $f16, 0($3) # a[i], load coefficient
      add.s f0, f16, f14 # y = a[i] + (x*y)
      addi $5, $5, -1 # decrease i
      beq $2, $0, Loop # goto Loop if i >= 0
Exit:
           $31
```

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        add.s f0, f16, f14 # y = a[i] + (x*y)
        addi $5, $5, -1 # decrease i
        slt $2, $5, $0 # $2 = 1 if i < 0
        beq $2, $0, Loop # goto Loop if i >= 0
Exit:
             $31
# Evaluate the value of a polynomial using Horner's algorithm.
# f = a[0] + a[1] * x + a[2] * x^2 + ... + a[n] * x^n
```



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'70s	Pascal('70), C ('72), Prolog('72), SQL('78), Matlab ('78)
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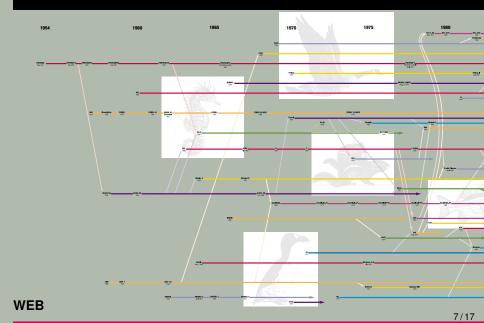
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Oldest programming language?

Plankalkül (1940s). For the Z1 computer, by Konrad Zuse.

History of Programming Languages



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- The program can then be **executed** separately, at a later time.
- The executable is portable only to compatible platforms. The program?
- Speed!
- Examples: C, Fortran.

Program:

sequence of instructions expressing the operations to be performed on a target computing platform.

 $\begin{array}{ll} \bullet & \text{Each program } \mathcal{P} \text{ has a meaning. It implements a function.} \\ & \{ \text{Initial State} \} & \mathcal{P} & \{ \text{Final State} \}. \end{array}$

Program:

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- \circ [[\mathcal{P}]] is the *semantics* of the program \mathcal{P} . [[]] = Semantics operator. Operational, Denotational, Axiomatic. Out of the scope of this class.
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- Remember: when working with floating point numbers, the expression x == y does not make sense!

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result := routine_name( arguments )
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BUT! One difference: side-effects.
 Many languages allow subroutines to have side-effects.
 The routine alters the state of the system even after its completion.

Side Effects

```
 \{ (res = ...) \land State \} 
 res := routine_name( args ); 
 \{ (res = ...) \land State' \}
```

- If (State = State') → no side-effects.
- Most languages allow constructs with side-effects.
- Print statements; iterative constructs; ...

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- Structure:

```
routine_name( args )
   //
  body
   //
return( value )
```

depending on the language, args, body and value are optional

Yes! → Recursion.

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Recursion ≡ iteration!

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- BLAS LAPACK PETSc MPI ...

 FFTW LINPACK OpenMP

 EISPACK Pthreads
- Libraries can be written in one or more languages.
 Can they be accessed from a program written in a different language?

Imperative vs. Functional Languages

Imperative Languages

- Concept of Variables and State.
- Program is an ordered sequence of commands and assignments.
- Commands modify state. Side-effects.
- C, C++, Fortran, Java, Python, Matlab, . . .

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Functional Languages

- No variables or assignments.
- Program consists of Functions and Recursion.
- No side-effects!
- Subset of Declarative Languages.
- Lisp, APL, ADA, Haskell, Mathematica, Clojure, F# . . .

```
Program A;
Var I:Integer;
    K:Char;
    R:Real;
    Procedure B;
    Var K:Real;
        L:Integer;
        Procedure C;
        Var M:Real;
        Begin
        // Body #1
        End;
    Begin
    // Body #2
    End;
Begin
// Body #3
End;
```

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I:Integer, R:Real, K:Real, L:Integer,
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• Where is K used as Real?

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• Where is K used as Real?

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Body #1 and Body #2
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Body #1 and Body #2
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Can L be referenced in Body #2? Body #3?

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Body #1 and Body #2
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Can L be referenced in Body #2? Body #3?

```
Body #2: yes; Body #3: no
```

```
program main
var y: Real;
    procedure compute()
    var x : Integer;
        procedure initialize()
        var y: Integer;
        var z: Real;
        begin {initialize}
        // Body #1
        end {initialize}
        procedure transform()
        var x: Real;
        begin {transform}
        // Body #2
        end {transform}
    begin {compute}
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begin {main}
// Main body
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y:Real and x:Real