

Genome-Wide Association Studies: Computing Petaflops over Terabytes of Data

Paolo Bientinesi

AICES, RWTH Aachen
pauldj@aices.rwth-aachen.de

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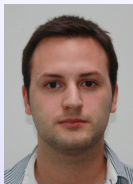


Acknowledgments



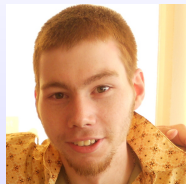
Yurii Aulchenko

Biologist



Diego Fabregat

Main developer



Lucas Beyer

GPUer

Deutsche
Forschungsgemeinschaft

DFG

- 1 The problem
- 2 Single trait analysis: $t = 1$
- 3 The complete multi-trait analysis: $t > 1$
- 4 Future work

Mixed models: $b := (X^T M^{-1} X)^{-1} X^T M^{-1} y$

Genome-wide association analysis

- y : phenotype
(outcome; vector of observations)
E.g.: height, blood pressure for a set of people
- X : genome measurements and covariates
(design matrix; predictors)
E.g.: sex and age over height
- M : dependencies between observations
E.g.: tall parents have tall children
- b : relation between a variation in the outcome (y)
and a variation in the genome sequence (X)

Linear regression with non-independent outcomes

$$b := (X^T M^{-1} X)^{-1} X^T M^{-1} y$$

Genome-wide association study

Inputs

- $M \in \mathcal{R}^{n \times n}$, $SPD(M)$, $n \in [10^3, \dots, 10^4]$
- $X \in \mathcal{R}^{n \times p}$, $p \in [3, \dots, 20]$, full rank
- $y \in \mathcal{R}^n$

Output

- $b \in \mathcal{R}^p$

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★To be repeated thousands of times★

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⇒

```
for( i=0; i < thousands_of_times; i++ )
{
    /* LOAD  problem_i */
    X = read( "file_X", n * p  , offset, ... );
    y = read( "file_y", n      , offset, ... );
    M = read( "file_M", n * n/2, offset, ... );
    // or maybe: M = generate_matrix( ... )

    /* SOLVE  problem_i */
    b = compute( X, M, y );

    /* STORE  solution_i */
    write( "file_b", b, p, offset, ... );
}
```

“To be repeated thousands of times”

⇒

- independent problem instances
 - computational cost: $O(n^3 + n^2p + np^2) = O(n^3)$

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- independent problem instances
 - computational cost: $O(n^3 + n^2p + np^2) = O(n^3)$
- access pattern irrelevant
- opportunity for overlapping computation and data movement
 - double buffering

The problem - the real setup

2D sequence

$$b_{ij} := (X_i^T M_j^{-1} X_i)^{-1} X_i^T M_j^{-1} y_j$$

$$\begin{aligned} i &= 1 \dots m, & \text{where } m &\approx 10^6 - 10^7 \\ j &= 1 \dots t, & \text{where } t &\text{ is either 1 or } \approx 10^5 \end{aligned}$$

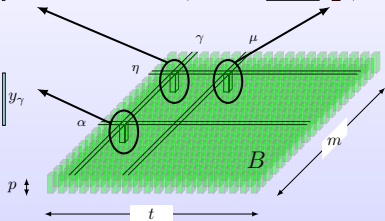
Also:

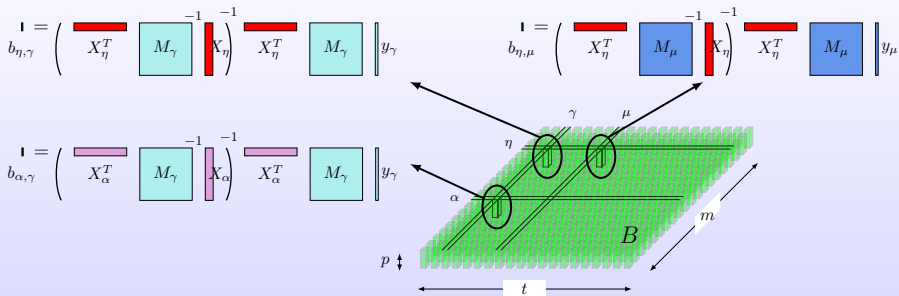
for each b_{ij} , compute and store $v_{ij} \in \mathcal{R}^{p \times p}$

$$b_{\eta,\gamma} = \left(\begin{array}{c} \text{---} \\ X_{\eta}^T \\ \text{---} \end{array} \begin{array}{c} -1 \\ M_{\gamma} \\ -1 \end{array} \begin{array}{c} -1 \\ X_{\eta} \\ -1 \end{array} \right) \begin{array}{c} \text{---} \\ X_{\eta}^T \\ \text{---} \end{array} \begin{array}{c} M_{\gamma} \\ \text{---} \end{array} \parallel y_{\gamma}$$

$$b_{\eta,\mu} = \left(\begin{array}{c} \text{---} \\ X_{\eta}^T \\ \text{---} \end{array} \begin{array}{c} -1 \\ M_{\mu} \\ -1 \end{array} \begin{array}{c} -1 \\ X_{\eta} \\ -1 \end{array} \right) \begin{array}{c} \text{---} \\ X_{\eta}^T \\ \text{---} \end{array} \begin{array}{c} M_{\mu} \\ \text{---} \end{array} \parallel y_{\mu}$$

$$b_{\alpha,\gamma} = \left(\begin{array}{c} \text{---} \\ X_{\alpha}^T \\ \text{---} \end{array} \begin{array}{c} -1 \\ M_{\gamma} \\ -1 \end{array} \begin{array}{c} -1 \\ X_{\alpha} \\ -1 \end{array} \right) \begin{array}{c} \text{---} \\ X_{\alpha}^T \\ \text{---} \end{array} \begin{array}{c} M_{\gamma} \\ \text{---} \end{array} \parallel y_{\gamma}$$





A completely different problem!

- data re-use
- cost depends on traversal
- HUGE datasets — Terabytes

Parameters

- n : population size
- m : number of SNP
- t : number of traits

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Scenario #1

$$t = 1$$

$$n = 10.000$$

$$m = 3.000.000$$

Input: 220 GBytes

Output: .2 GBytes

Cost: 3.000 Pflops

Scenario #2

$$t = 100.000$$

$$n = 1.000$$

$$m = 1.000.000$$

Input: 8 GBytes

Output: 9 TBytes

Cost: 100.000 Pflops

Scenario #3

$$t = 100.000$$

$$n = 10.000$$

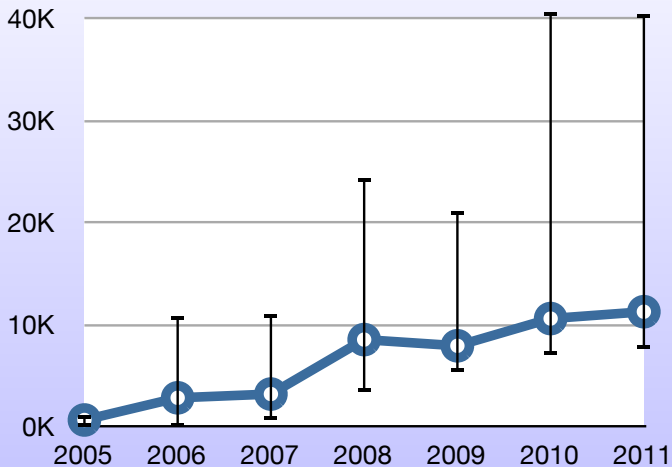
$$m = 10.000.000$$

Input: 750 GBytes

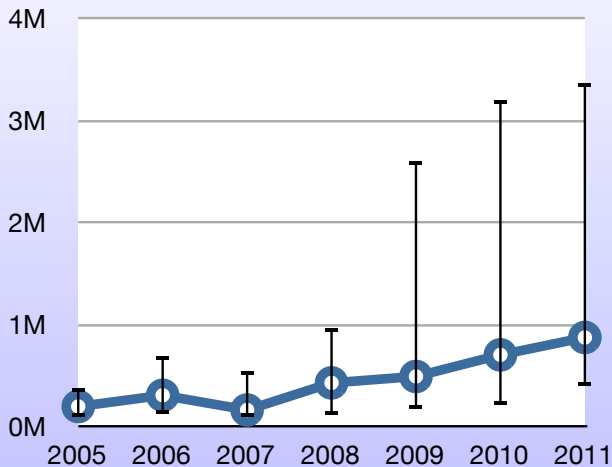
Output: 90 TBytes

Cost: 1.000.000 **Eflops**

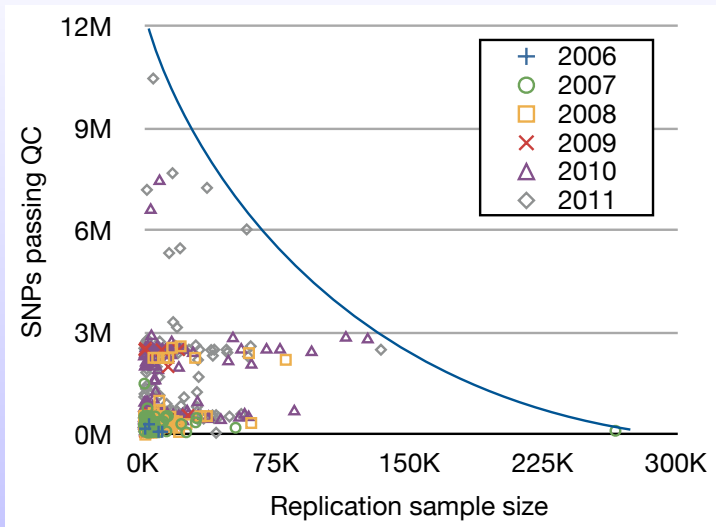
GWAS database: Population size – n



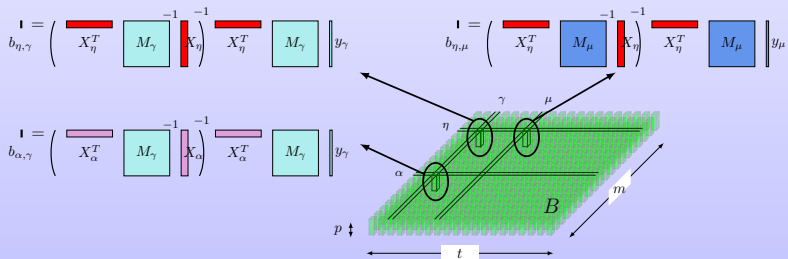
GWAS database: SNPs – m



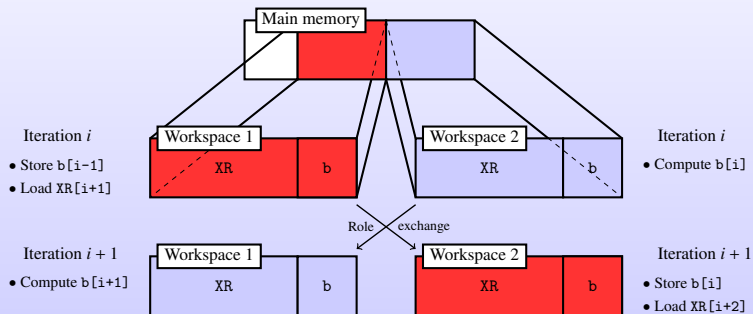
GWAS database: Population vs SNPs



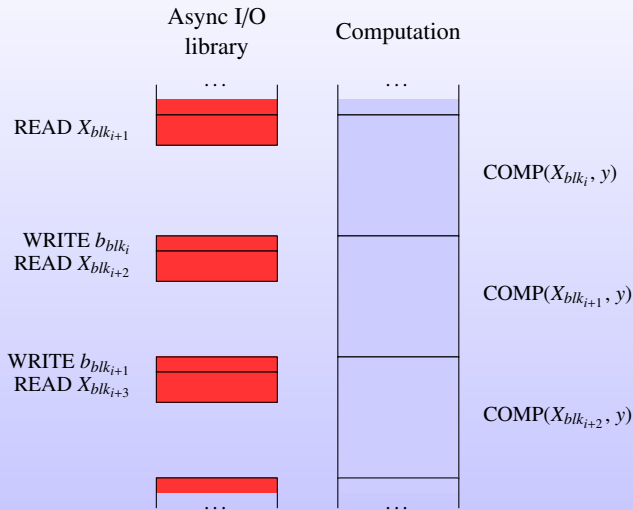
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Double buffering

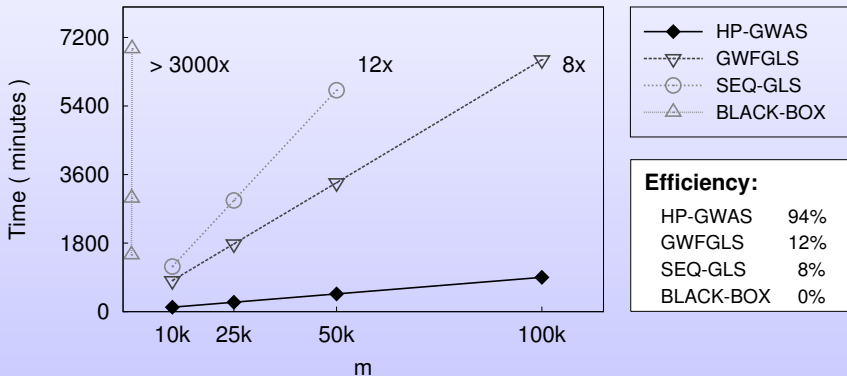


Overlap



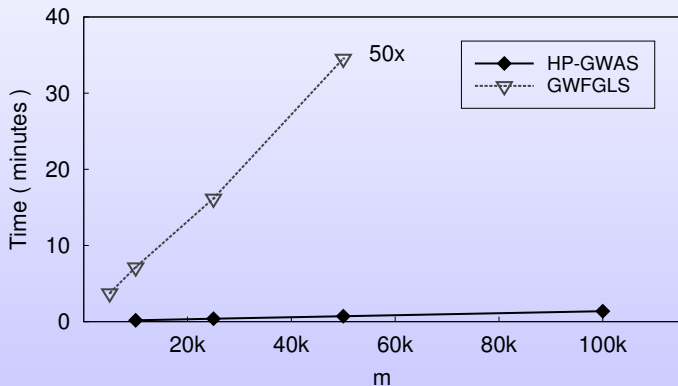
Our algorithm: HP-GWAS

Xeon, single thread $n = 10.000, p = 4$



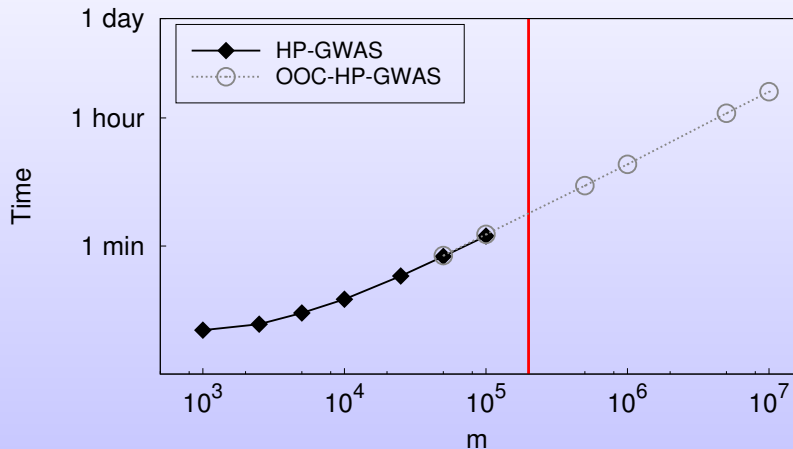
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Xeon, 12-cores $n = 10.000, p = 4$



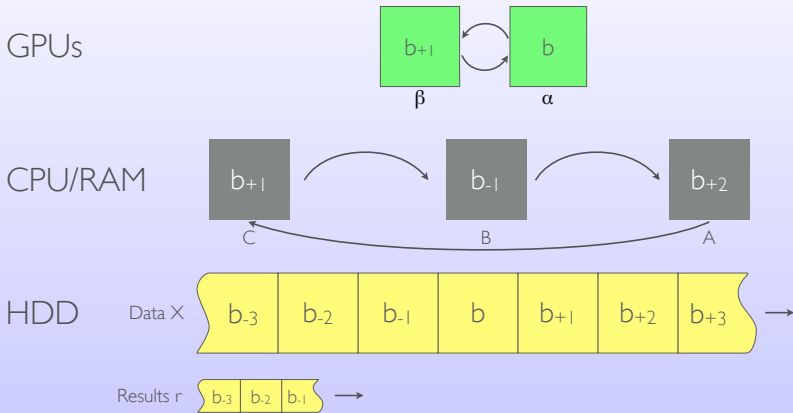
In-core vs Out-of-core

Main memory: 32GB $n = 10.000, p = 4$



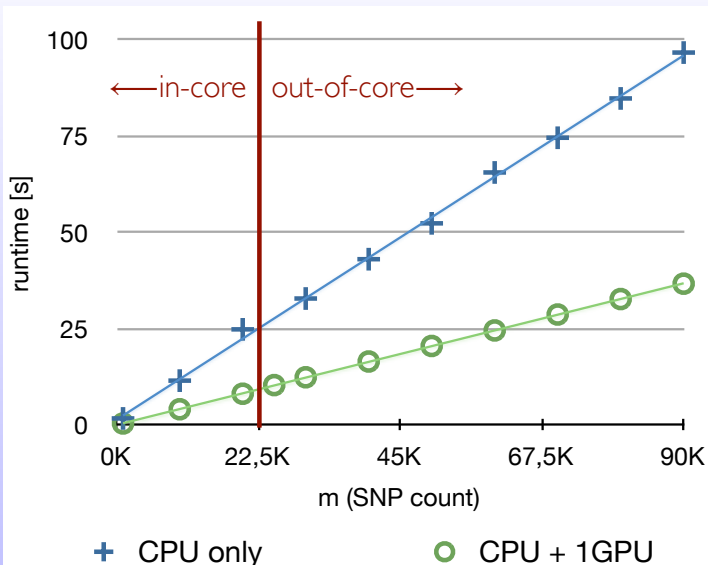
GPUs: Double+Triple buffering

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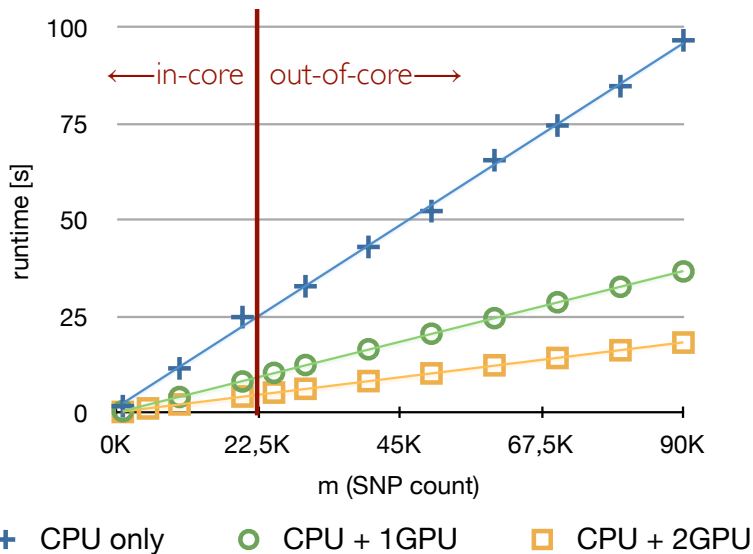


GPU: Results

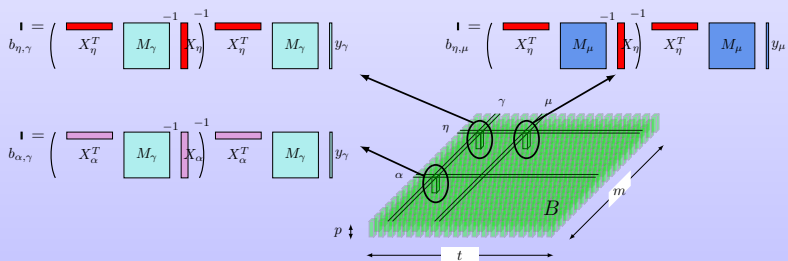
Main memory: 24GB, Fermi: 6GB $n = 10.000, p = 4$



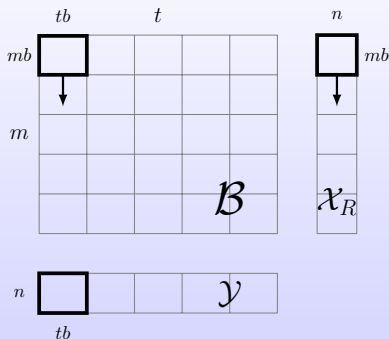
Multiple GPUs



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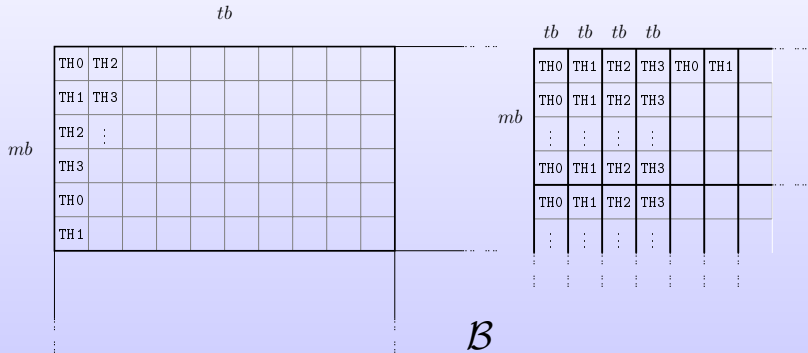


Degrees of freedom



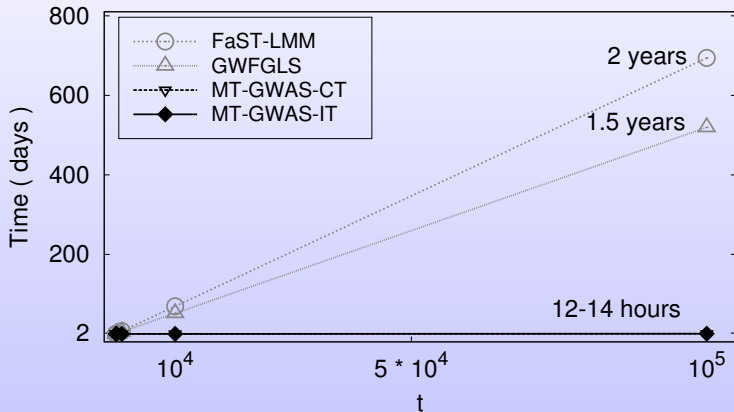
- I/O: How to traverse B ? (blocking / shape / direction)
- Single-threaded or collaborative I/O?
- Caching: How to use multi-threading? (blocking / shape)

I/O management



Results

Xeon, 512GB, 40 threads $n = 1.000, p = 4, m = 1.000.000$



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- $t = 1$: 40-fold speedups on 12 cores
- $t = 1$: k -fold speedup with k GPUs
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none of our I/O mechanisms will be accepted
- sacrifice overlap for filtering, casting, post-processing, ...

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TODO list

- Large n : distributed memory
- GPUs for multi-trait GWAS
- Exploit sparsity